

# ProgressCurve\_TimeCourse

January 12, 2022

Written by G. Gygli.

Contact [gudrun.gygli@kit.edu](mailto:gudrun.gygli@kit.edu) in case of questions.

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## 1 A time-course experiment

This script aims to help you design time-course experiments for *single-substrate, single-enzyme catalyzed reactions*.

Input: estimates of  $K_m$  and  $v_{\max}$  and indicate the enzyme concentration concentration ( $E_0$ ) and substrate concentration ( $s_0$ ) you are planning to use.

If you have no estimates to give, try the experiment with the suggested initial values.

This notebook is heavily based on the work by Stroberg and Schnell, and their recommendations for the design of time course experiments: <https://doi.org/10.1016/j.bpc.2016.09.004>

In order for both  $K_m$  and  $v_{\max}$  to be derived from substrate progress curve measurements: 1.  $s_0$  must be within approximately an order of magnitude of  $K_m$ .

a. If  $s_0 \gg K_m$ , a linear fit to the initial velocity will yield  $v_{\max}$ , but provide no information about  $K_m$ .

b. If  $s_0 \ll K_m$ , the ratio of  $v_{\max}$  to  $K_m$ , but neither parameter independently can be determined.

2.  $E_0$  must be smaller than the Michaelis constant, that is  $\frac{E_0}{K_m} \ll 1$  3. Data points should be collected around the time point where the time course curvature is at it highest. 4.  $E_0$  must be smaller than  $s_0$ . 5.  $E_0$  should be between 0.25 and 25  $K_m$ .

Finally, note that the equations used to simulate data are:

$$\frac{s(t)}{s_0} = \left(\frac{s_0}{K_m}\right)^{-1} W\left[\frac{s_0}{K_m} e^{\left(\frac{s_0}{K_m} - \frac{V}{K_m} t\right)}\right]$$

(which does not take into account  $E_0$ ).

And the the approximation taking into account  $E_0$ :

$$\frac{s(t)}{s_0} \approx e^{-\frac{k_{\text{cat}} E_0 t}{K_m} \left(1 - \frac{s_0}{k_{\text{cat}} E_0}\right)}$$

```
[1]: # Here, we import all the python packages we need to run this script.
# in the unlikely case they are not installed on your computer, this might help:
↪
# https://jakevdp.github.io/blog/2017/12/05/
↪ installing-python-packages-from-jupyter/
```

```

# accessed 04.10.21
import pandas
from scipy.special import lambertw
from scipy.optimize import curve_fit
import numpy as np
import scipy
import warnings
from scipy.optimize import OptimizeWarning
import matplotlib.pyplot as plt

# function to model
def Srt_schnell(t, Km: float, Vmax: float):
    # print("t,Km,Vmax",t,Km,Vmax)
    E = np.exp((s0/Km)-(Vmax/Km)*t)
    # L = np.abs(lambertw((s0/Km)*E)) # this apparently can be complex which
    ↳ can cause Errors
    # - the initial values given in the example below do not suffer from this
    ↳ problem, in case you
    # run into this problems, try using the line below instead,
    # where the output of the lambertw function is converted into an absolute
    ↳ value (using np.abs() )
    L = lambertw((s0/Km)*E) # this apparently can be complex which can cause
    ↳ Errors
    y = pow((s0/Km),-1)*L
    return y

def Srt_enzymeconcentrationdependent(t,E0, Km: float, Vmax: float):
    kcat=Vmax/E0
    y = np.exp((- (kcat*t*E0)/Km)*(1 - (s0/(kcat*E0*t))))
    return y

```

## 1.1 INPUT: Enzyme reaction parameters

Here, you can give an estimate of the enzyme reaction parameters  $K_m$  and  $v_{\max}$  for a **single-substrate, single-enzyme catalyzed reaction**. These parameters are needed to model data using the Michaelis-Menten equation, and can be adjusted as you progress with your experiments.

```

[2]: vmax = 10 # units: M/s, initial value: 10
    Km = 100 # units: M, initial value: 100

```

```

[3]: # we will be using a random noise generator to include some variation in our
    ↳ simulated data
    # fixing the seed for the random noise generation to always get the same result.
    ↳
    # comment this line if you want to always get different data.

```

```
np.random.seed(1) # initial value: 1
# noiselevelMM controls how "noisy" your fake data will be, but it has not real
↳ meaning for your actual experiment.
noiselevelMM = 1 # initial value: 1
```

## 1.2 INPUT: experimental conditions parameters

Choose how long you want to follow the reaction, i.e. how long your experiment should take by setting the length of  $t$  (units in the example are minutes, this obviously has consequences on the units of  $v_{\max}$ , and the x-axis in the plot). Units must be manually verified and adjusted if changes are made...

Note that besides  $t$  you also **MUST** give a starting concentration of substrate ( $s_0$ ) and a starting concentration of enzyme ( $E_0$ ).

```
[4]: t = list(range(0, 100)) # units: seconds, initial value: 100
# note: this line creates a list (array) filled with 100 elements, starting
↳ from 0 and ending with 100
s0 = 200 # units: M, initial value: 200
E0 = 25 # units: M, initial value: 25
```

Now, run all the code below to see what data you can expect to obtain for the input parameters you gave.

This is where the data are simulated and plotted. Depending on how the plot looks, you may want to adjust  $t$ ,  $s_0$  and  $E_0$ .

Note that  $v_{\max}$  influences how quickly the reaction is over. Because  $v_{\max}$  is a property of the enzyme, we need to shorten  $t$  for high  $v_{\max}$ , and lengthen  $t$  for low  $v_{\max}$ .

## 1.3 The approximation

used to simulate data taking into account  $E_0$  leads to unrealistic behaviour for small  $t$  s: in the beginning of your simulated experiment, you can observe substrate concentrations that are  $\gg s_0$  (uncomment line 31 in the code below to fully see the effect). This is certainly not realistic, but shows you that the curvature of your data can change in this case.

```
[5]: # some preparations:
v0 = t.copy() # initialize the array, the values will be overwritten later
v1 = t.copy() # initialize the array, the values will be overwritten later

# fixing the seed for the random noise generation to always get the same result.
↳
# comment this line if you want to always get different data.
np.random.seed(1) # initial value: 1

#create a figure with satisfactory dimensions and resolution:
fig = plt.figure(figsize=[5,3], dpi=500)

# This code is repeated again and again below.
```

```

# It is not put into a function to enable beginners in Python programming to
↳ understand what is happening.
for i in t:
    if i==0:
        v0[i]=s0
    else:
        v0[i] = s0*Srt_schnell(i,Km,vmax)
        noise = noiselevelMM*(np.random.random(1)-0.5)
        data_random = v0[i] + noise

for i in t:
    if i==0:
        v1[i]=s0
    else:
        #using your E0 given above as input
        v1[i] = s0*Srt_enzymeconcentrationdependent(i,E0,Km,vmax)
        noise = noiselevelMM*(np.random.random(1)-0.5)
        data_random = v1[i] + noise

# plt.ylim(ymax = s0+(s0/10), ymin = 0-(s0/10))
#fixing the axis so that in case of very bad initial parameter choices we do
↳ not get confused by [S]>>[S0]

plt.scatter(t,v0,label="not taking [E_0$] into account", facecolors='none',
↳ edgecolors='black',s=20)
plt.scatter(t,v1,label="using [E_0$]=25", facecolors='none',
↳ edgecolors='yellow',s=20)

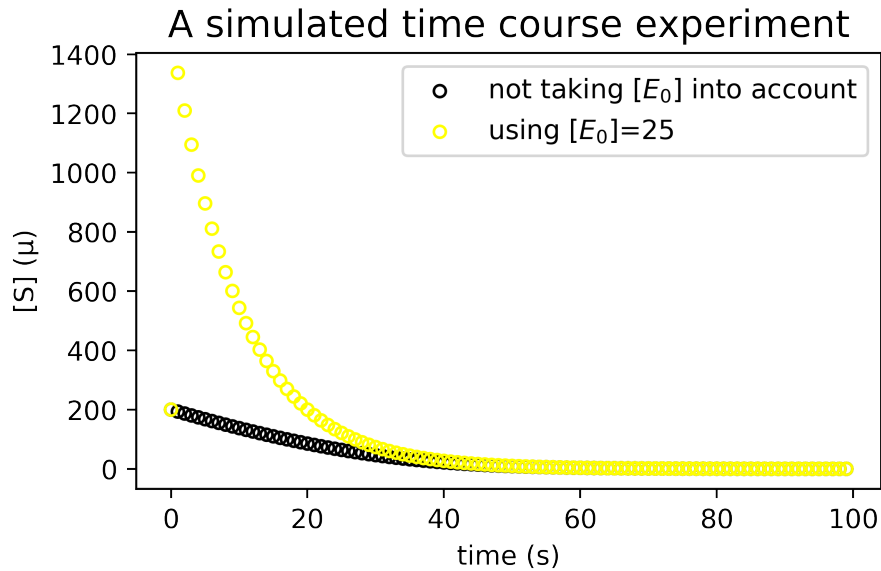
plt.title("A simulated time course experiment", fontsize=14)
plt.legend(loc='upper right')

plt.ylabel('[S] (\u03BC)')
plt.xlabel('time (s)')

```

C:\Users\Gudrun\anaconda3\lib\site-packages\numpy\core\\_asarray.py:138:  
ComplexWarning: Casting complex values to real discards the imaginary part  
return array(a, dtype, copy=False, order=order, subok=True)

[5]: Text(0.5, 0, 'time (s)')



If we now check if we fulfill the criteria by Stroberg and Schnell, we see that there are some issues to deal with:

1. The  $s_0$  must be within approximately an order of magnitude of the Michaelis constant.  
TRUE:  $s_0 = 200 \text{ M}$ ,  $K_m = 100 \text{ M}$
2.  $E_0/K_m \ll 1$   
TRUE for low  $E_0$ :  $E_0 = 0.25 \cdot 100 = 25 \rightarrow 25/100 \ll 1$   
FALSE for high  $E_0$ :  $E_0 = 25 \cdot 100 = 2500 \rightarrow 2500/100 \gg 1$
3. Data points should be collected around the time point where the time course curvature is at it highest.  
here, we need to sample better...
4.  $E_0$  must be smaller than  $s_0$ .  
TRUE for low  $E_0$ , but false for high low  $E_0$
5.  $E_0$  should be between 0.25 and 25  $K_m$ . TRUE

#### 1.3.1 Now it is up to you:

you can try what happens if you adjust  $E_0$ ,  $s_0$  **and**  $t$  in the code below. Make sure to adjust the units and info in the plot axes and legend.

```
[6]: t = list(range(0, 200)) # units: seconds (?)
# note: this line creates a list (array) filled with 100 elements, starting
# from 0 and ending with 100
s0 = 100 # units: M (?)
E0 = 1 # units: M (?)
```

```

# some preparations:
v0 = t.copy() # initialize the array, the values will be overwritten later
v1 = t.copy() # initialize the array, the values will be overwritten later

# fixing the seed for the random noise generation to always get the same result.
→
# comment this line if you want to always get different data.
np.random.seed(1) # initial value: 1

#create a figure with satisfactory dimensions and resolution:
fig = plt.figure(figsize=[5,3], dpi=500)

# This code is repeated again and again below.
# It is not put into a function to enable beginners in Python programming to
→understand what is happening.
for i in t:
    if i==0:
        v0[i]=s0
    else:
        v0[i] = s0*Srt_schnell(i,Km,vmax)
        noise = noiselevelMM*(np.random.random(1)-0.5)
        data_random = v0[i] + noise

for i in t:
    if i==0:
        v1[i]=s0
    else:
        #using your E0 given above as input
        v1[i] = s0*Srt_enzymeconcentrationdependent(i,E0,Km,vmax)
        noise = noiselevelMM*(np.random.random(1)-0.5)
        data_random = v1[i] + noise

# plt.ylim(ymax = s0+(s0/10), ymin = 0-(s0/10))
#fixing the axis so that in case of very bad initial parameter choices we do
→not get confused

plt.scatter(t,v0,label="not taking [E_0$] into account", facecolors='none',
→edgecolors='black',s=20)
plt.scatter(t,v1,label="using [E_0$]= ???", facecolors='none',
→edgecolors='yellow',s=20)

plt.title("Another simulated time course experiment", fontsize=14)
plt.legend(loc='upper right')

plt.ylabel('[S] (???)')
plt.xlabel('time (???)')

```

```
[6]: Text(0.5, 0, 'time (???)')
```

